

Problem 27.11

a.) The current density (current per unit area) is:

$$\begin{aligned} J &= \frac{I}{A} = \frac{8 \times 10^{-6} \text{ A}}{\pi (10^{-3} \text{ m})^2} \\ &= 2.55 \text{ A/m}^2 \end{aligned}$$

b.) From Problem 27.3, we can write the electron density n as:

$$\begin{aligned} I &= nqAv_d \\ \Rightarrow J &= \frac{I}{A} = nev_d \\ \Rightarrow n &= \frac{J}{ev_d} \\ \Rightarrow &= \frac{(2.55 \text{ A/m}^2)}{(1.6 \times 10^{-19} \text{ C})(3 \times 10^8 \text{ m/s})} \\ \Rightarrow &= 5.3 \times 10^{10} \text{ m}^{-3} \end{aligned}$$

c.) How long will Avogadro's number of electrons exit the accelerator?

$$I = \frac{\Delta q}{\Delta t}$$

$$\begin{aligned}\Rightarrow \Delta t &= \frac{\Delta q}{I} \\ &= \frac{(N_{\text{Avogadro}} e)}{I} \\ &= \frac{(6.02 \times 10^{23})(1.6 \times 10^{-19} \text{ C})}{(8 \times 10^{-6} \text{ A})} \\ &= 1.2 \times 10^{10} \text{ seconds}\end{aligned}$$